



GAUTENG PROVINCE
EDUCATION
REPUBLIC OF SOUTH AFRICA

JUNE EXAMINATION
GRADE 12

2024

MARKING GUIDELINES

MATHEMATICS

(PAPER 1)

12 pages

NOTE:

Read the following instructions carefully before answering the questions.

- If a candidate answers a question TWICE, only mark the first attempt.
- If a candidate has crossed OUT an answer and did not redo it, mark the crossed-out answers.
- Consistent accuracy applies in ALL aspects of the marking guidelines
- Assuming values/answers in order to solve a question is UNACCEPTABLE.

QUESTION 1				
1.1	1.1.1	$2x(3x + 4) = 0$ $x = 0$ or $x = -\frac{4}{3}$	✓ $x = 0$ ✓ $x = -\frac{4}{3}$	(2)
	1.1.2	$2x^2 - 4x + 1 = 0$ $x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(2)(1)}}{(2)(2)}$ $x = \frac{4 \pm \sqrt{8}}{4}$ $x = 1,71$ or $x = 0,29$	✓ standard form ✓ substitute into correct formula ✓ $x = 1,71$ ✓ $x = 0,29$ [-1 for incorrect rounding only in this question]	(4)
	1.1.3	$(x - 2)^2 \geq 1$ $x^2 - 4x + 4 \geq 1$ $x^2 - 4x + 3 \geq 0$ $(x - 3)(x - 1) \geq 0$ CV $x = 3$ or $x = 1$ $x \leq 1$ or $x \geq 3$ Or $(x - 2) \leq -1$ or $(x - 2) \geq 1$ $x \leq -1 + 2$ or $x \geq 1 + 2$ $x \leq 1$ or $x \geq 3$	✓ standard form ✓ factors ✓ critical values ✓ answer ✓✓ correct inequalities with square rooting both sides ✓ simplifying ✓ answer	(4)
1.2	1.2.1	$\sqrt{x - 2} = 4 - x$ $x - 2 \geq 0$ and $4 - x \geq 0$ $x \geq 2$ and $x \leq 4$ $2 \leq x \leq 4$	✓ $x - 2 \geq 0$ ✓ $4 - x \geq 0$	(2)
	1.2.2	$\sqrt{x - 2} = 4 - x$ $x - 2 = 16 - 8x + x^2$ $x^2 - 9x + 18 = 0$ $(x - 6)(x - 3) = 0$ $x \neq 6$ or $x = 3$	✓ square both sides ✓ standard form ✓ factors ✓ selecting $x = 3$	(4)

<p>1.3</p>	<p> $3x + y = 2$ and $y^2 = 2x^2 - 1$ Equation 1. $y = 2 - 3x$ $(2 - 3x)^2 = 2x^2 - 1$ $4 - 12x + 9x^2 = 2x^2 - 1$ $7x^2 - 12x + 5 = 0$ $(7x - 5)(x - 1) = 0$ $x = \frac{5}{7}$ or $x = 1$ $y = -\frac{1}{7}$ or $y = -1$ OR Equation 1 $x = \frac{2-y}{3}$ $y^2 = 2 \left(\frac{2-y}{3} \right)^2 - 1$ $y^2 = 2 \left(\frac{4 - 4y + y^2}{9} \right) - 1$ $9y^2 = 8 - 8y + 2y^2 - 9$ $7y^2 + 8y + 1 = 0$ $(7y + 1)(y + 1) = 0$ $y = -\frac{1}{7}$ or $y = -1$ $x = \frac{5}{7}$ or $x = 1$ </p>	<ul style="list-style-type: none"> ✓ subject of equation ✓ substitution ✓ standard form ✓ factors ✓ x-values ✓ y-values
<p>1.4</p>	<p> $r + 2s = a$ $r + 2s = a$ $r - 2s = b$ $r - 2s = b$ $2r = a + b$ $4s = a - b$ $r = \frac{a+b}{2}$ $s = \frac{a-b}{4}$ $rs = \frac{a^2 - b^2}{8}$ OR $RHS = \frac{a^2 - b^2}{8}$ $= \frac{(r + 2s)^2 - (r - 2s)^2}{8}$ $= \frac{(r^2 + 4rs + 4s^2) - (r^2 - 4rs + 4s^2)}{8}$ $= \frac{8rs}{8}$ $= rs$ </p>	<ul style="list-style-type: none"> ✓ $2r = a + b$ ✓ $4s = a - b$ ✓ r and s subject of equation ✓ multiplication <p>OR</p> <ul style="list-style-type: none"> ✓ substitution of a and b ✓ expand ✓ simplify

(6)

(4)

[26]

QUESTION 2

2.1	2.1.1	$85 ; 82 ; 79 ; 76$ $a = 85 \quad d = -3$ $T_n = a + (n - 1)d$ $T_n = 85 + (n - 1)(-3)$ $T_n = 85 - 3n + 3$ $T_n = 88 - 3n$	✓ d value ✓ substitute a and d ✓ answer	(3)
	2.1.2	$T_n = 88 - 3n < 0$ $-3n < -88$ $n > \frac{88}{3}$ $\therefore T_{30}$ will be the first negative number.	✓ $T_n < 0$ ✓ simplify ✓ answer Answer only full marks	(3)
2.2		$T_n - T_{n-1} = 4n - 3$ $\therefore T_1 = 4(2) - 3 = 5 \quad T_2 = 4(3) - 3 = 9 \quad T_3 = 4(4) - 3 = 13$ First difference = 5 ; 9 ; 13 Second difference = 4 ; 4 $2a = 4 \quad 3a + b = 5$ $a = 2 \quad 3(2) + b = 5$ $b = -1$ $T_{11} = 190$ $T_n = 2n^2 - 1n + c$ $190 = 2(11)^2 - 1(11) + c$ $190 = 242 - 11 + c$ $c = -41$ $T_n = 2n^2 - n - 41$ $T_1 = 2(1)^2 - (1) - 41 = -40$	✓ first difference ✓ value of a ✓ value of b ✓ value of c ✓ value of T_1	(5)
		OR	OR	

	$T_n = an^2 + bn + c$ $T_{n-1} = a(n-1)^2 + b(n-1) + c$ $T_n - T_{n-1} = an^2 + bn + c - [a(n^2 - 2n + 1) + bn - b + c]$ $= an^2 + bn + c - an^2 + 2an - a - bn + b - c$ $= 2an - a + b$ $2an - a + b = 4n - 3$ $2a = 4$ $a = 2$ $-a + b = -3$ $-2 + b = -3$ $b = -1$ $121(2) + 11(-1) + c = 190$ $c = -41$ $T_n = 2n^2 - n - 41$ $T_1 = 2(1)^2 - (1) - 41 = -40$	<ul style="list-style-type: none"> ✓ expanding T_{n-1} ✓ value of a ✓ value of b ✓ value of c ✓ value of T_1
2.3	$S_n = \frac{n}{2}[2a + (n-1)d]$ $1275 = \frac{50}{2}[2a + (50-1)d]$ $51 = [2a + 49d]$ $T_{25} + T_{26} = a + 24d + a + 25d$ $T_{25} + T_{26} = 2a + 49d$ $T_{25} + T_{26} = 51$	<ul style="list-style-type: none"> ✓ substitute in formula ✓ expanding $T_{25} + T_{26}$ ✓ answer
QUESTION 3		
3.1	$\sum_{k=1}^{\infty} (4x-1)^k$ $(4x-1)^1 + (4x-1)^2 + (4x-1)^3 \dots$ $r = (4x-1)$ $-1 < r < 1$ $-1 < 4x-1 < 1$ $0 < 4x < 2$ $0 < x < \frac{1}{2} \quad x \neq \frac{1}{4}$	<ul style="list-style-type: none"> ✓ r ✓ condition ✓ answer ✓ excluding $x \neq \frac{1}{4}$
3.2	<p>3.2.1 $T_1 = 3$ and $T_5 = 48$</p> $T_n = ar^{n-1}$ $48 = 3 \cdot r^4$ $16 = r^4$ $\therefore r = 2$	<ul style="list-style-type: none"> ✓ sub into formula ✓ simplify ✓ answer

(3)
[14]

(4)

(3)

<p>3.2.2</p>	<p>Sum of radii for 5 circles</p> $S_n = \frac{a(r^n - 1)}{r - 1}$ $S_5 = \frac{3(2^5 - 1)}{2 - 1} = 93 \text{ units}$ $L = 93 \times 2 = 186 \text{ units}$ <p style="text-align: center;">OR</p> <p>Sum of diameter for 5 circles</p> $S_5 = \frac{a(r^n - 1)}{r - 1}$ $S_5 = \frac{6(2^5 - 1)}{2}$ $S_5 = 186$ $L = 186 \text{ units}$ <p style="text-align: center;">OR</p> $6 + 12 + 24 + 48 + 96 = 186$	<p>✓ subt in formula</p> <p>✓ simplify</p> <p>✓ answer</p>
<p>3.2.3</p>	<p>$\pi 3^2 + \pi \cdot 6^2 + \pi \cdot 12^2 + \dots$ to 10 terms</p> $r = \frac{\pi \cdot 6^2}{\pi \cdot 3^2}$ $r = 4$ $S_{10} = \frac{9\pi(4^{10} - 1)}{4 - 1}$ $S_{10} = 3\pi(1\ 048\ 575)$ $S_{10} = 3\ 145\ 725\pi$	<p>✓ area of circle</p> <p>✓ r value</p> <p>✓ subt into formula</p> <p>✓ answer</p>
<p>[16]</p>		

QUESTION 4

<p>4.1</p>	<p>$y = x + 1$ and $y = -x + 3$</p> $x + 1 = -x + 3$ $2x = 2$ $x = 1$ $y = 1 + 1$ $y = 2$ $p = -1$ $q = 2$	<p>✓ $x + 1 = -x + 3$</p> <p>✓ x-value</p> <p>✓ y-value</p>
<p>(3)</p>		

QUESTION 5

5.1	5.1.1	$f(x) = -(x - 2)^2 + 9$ $0 = -x^2 + 4x - 4 + 9$ $0 = x^2 - 4x - 5$ $(x - 5)(x + 1) = 0$ $x = 5$ or $x = -1$ $AC = 6$ units <p style="text-align: center;">OR</p> $(x - 2)^2 = 9$ $x - 2 = \pm 3$ $x - 2 = 3$ or $x - 2 = -3$ $x = 5$ or $x = -1$ $AC = 6$ units	✓ let $y = 0$ ✓ standard form ✓ x -values ✓ 6 units <p style="text-align: center;">OR</p> ✓ let $y = 0$ ✓ $(x - 2)^2 = 9$ ✓ x -values ✓ 6 units	(4)
	5.1.2	$D(2:9)$ $y = b^x$ $9 = b^2$ $b = 3$	✓ sub in $g(x)$ ✓ $b = 3$	(2)
	5.1.3	$x \geq 2$	✓ answer	(1)
	5.1.4	$f(x) = -(x - 2)^2 + 9$ $y = -(x + 2 - 2)^2 + 9 - 9$ $y = -x^2$	✓ subst ✓ answer Answer only full marks	(2)
	5.1.5	$x \leq 0$ or $x \geq 0$	✓ answer (accuracy mark)	(1)
	5.1.6	Prove: $g\left(x + \frac{1}{2}\right) = \sqrt{3}g(x)$ $g(x) = 3^x$ $g\left(x + \frac{1}{2}\right) = 3^{x+\frac{1}{2}}$ $= 3^x \cdot 3^{\frac{1}{2}}$ $= \sqrt{3}g(x)$	✓ subst ✓ use of exp law	(2)
5.2		$y = a(x - x_1)(x - x_2)$ $y = a(x + 3)(x - 2)$ $y = ax^2 + ax - 6a$ $y = mx + c$ $0 = m(-6) + c$ $0 = m(-6) - 6a$ $6a = -6m$ $a = -m$ OR	✓ subst in formula ✓ simplifying ✓ subst in formula ✓ subst c in formula ✓ $a = -m$	(5)

$$x = \frac{-3+2}{2} = -\frac{1}{2}$$

$$f'(x) = 2ax + b$$

$$0 = 2\left(-\frac{1}{2}\right)a + b$$

$$a = b$$

$$(-6; 0) (0; c)$$

$$m = \frac{c}{6}$$

$$c = 6m$$

$$0 = 4a + 2b + 6m$$

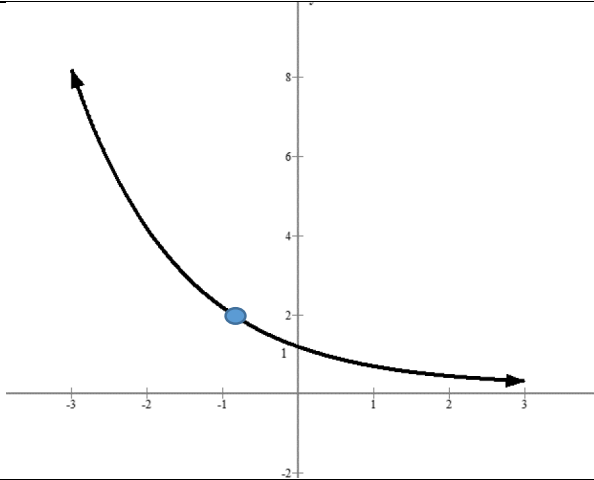
$$0 = 4a + 2a + 6m$$

$$-6a = 6m$$

$$a = -m$$

[17]

QUESTION 6

6.1	$A(1; 0)$	✓ $x = 1$	(1)
6.2	$x > 0$	✓ answer	(1)
6.3	$y = \log_{\frac{1}{2}} x$ $x = \log_{\frac{1}{2}} y$ $y = \left(\frac{1}{2}\right)^x$	✓ swop x and y ✓ answer Answer only full marks	(2)
6.4		✓ shape ✓ y-intercept ✓ one other point	(3)
6.5	$y = \log_{\frac{1}{2}} x$ $y = \log_{\frac{1}{2}} \frac{1}{2}$ $y = 1$	✓ answer	(1)

6.6	Reflection in the y-axis and translated one unit down	✓ reflection in y-axis ✓ translate one down
(2)		
[10]		

QUESTION 7

7.1	$1 + i_{eff} = \left(1 + \frac{i_{nom}}{m}\right)^m$ $i_{eff} = \left(1 + \frac{0,075}{4}\right)^4 - 1$ $r = 7,71\%$	✓ sub into formula ✓ simplify ✓ answer (accept i=0.0771)
(3)		

7.2	$A = P(1 - i)^n$ $4\ 200 = 60\ 000(1 - i)^{42}$ $\frac{4\ 200}{60\ 000} = (1 - i)^{42}$ $\sqrt[42]{\frac{4\ 200}{60\ 000}} = 1 - i$ $i = 1 - \sqrt[42]{\frac{4\ 200}{60\ 000}}$ $r = 6,14\%$	✓ n-value ✓ sub in form ✓ simplify ✓ r = 6,14% (accept in i form)
(4)		

7.3	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="text-align: center; width: 33%;">T0</td> <td style="text-align: center; width: 33%;">T3</td> <td style="text-align: center; width: 33%;">T10</td> </tr> <tr> <td style="text-align: center;">27000</td> <td style="text-align: center;">x</td> <td style="text-align: center;">17614.76</td> </tr> </table> $A = P \left(1 + \frac{i}{m}\right)^{n \times m}$ $17\ 614,76 = P \left(1 + \frac{0,054}{12}\right)^{7 \times 12}$ $P = R12\ 080,41$ $12\ 080,41 + x = 27\ 000 \left(1 + \frac{0,054}{12}\right)^{3 \times 12}$ $12\ 080,41 + x = 31\ 736,69$ $x = R19\ 656,28$ <p>OR</p>	T0	T3	T10	27000	x	17614.76	✓ substitution (3 years) ✓ answer ✓ substitutions ✓ simplify ✓ answer Or
T0	T3	T10						
27000	x	17614.76						
(5)								

$17\ 614,76 = 27\ 000\left(1 + \frac{0,054}{12}\right)^{120} - x\left(1 + \frac{0,054}{12}\right)^{84}$ $x\left(1 + \frac{0,054}{12}\right)^{84} = 27\ 000\left(1 + \frac{0,054}{12}\right)^{120} - 17\ 614,76$ $x = R19\ 656,28$	✓ $i = \frac{0,054}{12}$ ✓ $n = 120$ ✓ $-x$ ✓ $n = 84$ ✓ answer
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[12]

QUESTION 8 - Only penalise 1 mark for incorrect notation 8.1

8.1	$f(x) = 2 - 3x^2$ $f(x+h) = 2 - 3(x+h)^2$ $f(x+h) = 2 - 3x^2 - 6xh - 3h^2$ $f'(x) = \lim_{h \rightarrow 0} \frac{2 - 3x^2 - 6xh - 3h^2 - (2 - 3x^2)}{h}$ $= \lim_{h \rightarrow 0} \frac{-6xh - 3h^2}{h}$ $= \lim_{h \rightarrow 0} \frac{h(-6x - 3h)}{h}$ $= \lim_{h \rightarrow 0} (-6x - 3h)$ $= -6x$	✓ $f(x+h)$ ✓ substitution ✓ factors ✓ simplify ✓ answer	(5)	
8.2	8.2.1	$f(x) = 2x^4 - 3x + a^2$ $f'(x) = 8x^3 - 3$	✓ $8x^3$ ✓ -3 ✓ 0 (implied)	(3)
	8.2.2	$D_x \left[\frac{2x^3 - \sqrt{x}}{x} \right]$ $D_x \left[2x^2 - x^{-\frac{1}{2}} \right]$ $= 4x + \frac{1}{2}x^{-\frac{3}{2}}$	✓ $D_x \left[2x^2 - x^{-\frac{1}{2}} \right]$ ✓ $4x$ ✓ $\frac{1}{2}x^{-\frac{3}{2}}$	(3)
8.3	$y = mx + c$ $y = 7x + c$ $5 = 7(4) + c$ $c = -23$ $y = 7x - 23$ OR $y - 5 = 7(x - 4)$ $y - 5 = 7x - 28$ $y = 7x - 23$	✓ gradient ✓ subt ✓ equation	(3)	

QUESTION 9		
9.1	$f(x) = 2x^3 + px^2 + qx + 3 \quad N(2;-9)$ $-9 = 2(2)^3 + p(2)^2 + q(2) + 3$ $-9 = 16 + 4p + 2q + 3$ $-28 = 4p + 2q \dots\dots\textcircled{1}$ $f'(x) = 6x^2 + 2px + q$ $0 = 6(2)^2 + 2p(2) + q$ $0 = 24 + 4p + q$ $-24 = 4p + q \dots\dots\textcircled{2}$ Equation $\textcircled{1} - \textcircled{2}$ $\therefore -4 = q$ $-24 = 4p - 4$ $4p = -20$ $p = -5$	✓ sub in f ✓ $f(x) = 0$ ✓ sub in f' ✓ solve for q ✓ solve for p
		(5)
9.2	G(0;3)	✓ y-value 3 ✓ x-value 0
		(2)
9.3	$f(x) = 2x^3 - 5x^2 - 4x + 3$ $0 = (x - 3)(2x^2 + x - 1)$ $0 = (x - 3)(2x - 1)(x + 1)$ $x = 3 \text{ or } x = \frac{1}{2} \text{ or } x = -1$ AB = 1,5 units	✓ $(2x^2 + x - 1)$ ✓ factors ✓ roots ✓ 1,5
		(4)
9.4	$f'(x) = 6x^2 - 10x - 4$ $0 = 3x^2 - 5x - 2$ $(3x + 1)(x - 2) = 0$ $x = -\frac{1}{3}$	✓ $f'(x)$ ✓ factors ✓ x value
		(3)
9.5	$f''(x) = 12x - 10$ $0 = 12x - 10$ $x = \frac{10}{12} = \frac{5}{6}$ OR $x = \frac{-\frac{1}{3} + 2}{2}$ $x = \frac{5}{6}$ OR	✓ f'' ✓ = 0 ✓ $\frac{5}{6}$
		(3)

	$y'' = 6ax + 2b = 0$ $6ax = -2b$ $x = -\frac{2b}{6a}$ $x = \frac{-2(-5)}{6(2)} = \frac{5}{6}$		
9.6	$f'' > 0$ $6x - 5 > 0$ $x > \frac{5}{6}$	$\checkmark x > \frac{5}{6}$	(1)
9.7	$x < -1 \text{ or } -\frac{1}{3} < x < \frac{1}{2} \text{ or } 2 < x < 3$	$\checkmark x < -1$ $\checkmark -\frac{1}{3} < x < \frac{1}{2}$ $\checkmark 2 < x < 3$	(3)
			[21]

QUESTION 10			
10.1	10.1.1	$P(S \text{ and } T) = \frac{1}{6}$ $P(\text{not } S) = \frac{3}{4}$ $P(S) = \frac{1}{4}$ $P(S \text{ and } T) = P(S) \times P(T)$ $\frac{1}{6} = \frac{1}{4} \times P(T)$ $P(T) = \frac{2}{3}$	<p>✓ $P(S)$</p> <p>✓ subst in formula</p> <p>✓ $P(T)$</p>
			(3)
	10.1.2	$P(S \text{ or } T) = P(S) + P(T) - P(S \text{ and } T)$ $P(S \text{ or } T) = \frac{1}{4} + \frac{2}{3} - \frac{1}{6}$ $P(S \text{ or } T) = \frac{3}{4}$	<p>✓ sub into formula</p> <p>✓ answer</p>
			(2)
	10.2.1		<p>✓ Branch B or C 30% and 65%</p> <p>✓ Branch B or C 30% and 70%</p> <p>✓ outcomes</p>
			(3)
10.2	10.2.2	$P(\text{same meal}) = (0,35)(0,30) + (0,65)(0,70)$ $P(\text{same meal}) = 0,105 + 0,455 = 0,56$ $\text{Number of people} = 200 \times 0,56 = 112$	<p>✓ $(0,35)(0,30) + (0,65)(0,7)$</p> <p>✓ 0,56</p> <p>✓ 112</p>
			(3)
			[11]

TOTAL: 150